## **LECTURE SUMMARY 8**

## WEDNESDAY, JUN 29, 2016

## AUTONOMOUS DIFFERENTIAL EQUATIONS AND EQUILIBRIUM SOLUTIONS

- 1. Autonomous differential equations.
- 2. Equilibrium solutions.
- 3. Stability of equilibrium value.
- 4. Examples using MATLAB to show direction fields.
- 5. Examples of finding equilibrium solutions and assess the stability of each.
- 6. Theorem of determine stability of equilibrium values.
- 7. Convexity and Concavity.
- 8. Inflection points.

9. y'' = f'(y)f(y).

Applications: Logistic Growth Model and Logistic Growth Model with a Threshold

- $\begin{array}{ll} 1. \ y' = ky(1-\frac{y}{L}), \, \text{where} \ k, L > 0. \\ 2. \ y' = ky(1-\frac{y}{L})(\frac{y}{T}-1), \, \text{where} \ k > 0, 0 < T < L. \end{array}$
- 3. Explain how the population grows/decreases and how those coincide with solutions of the models.